





# Policy for written calculations -Mathematics

Date: February 2018

# **Document summary**

This document sets out the agreed progression from mental methods through to standard formal written calculations.

At all stages it is important that teaching is supported with structured models and images so that concepts can be embedded. This will be implemented by all age groups using concrete, pictorial and abstract within mathematics teaching.

It is more important that pupils understand what they are doing and can apply their 'method' to a given situation, than it is simply to be able to complete a standard written method.

We also agree to use precise mathematical vocabulary and encourage children to do the same.

We know that it is important to offer calculations in a range of representations. This is to include part, part whole; bar modelling; the tens frame; missing numbers and expressions where the = sign is not always in the traditional place.

This document should be read in conjunction with the 'Mathematics Policy'.

Woodlands Federation – Calculations Policy

	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Addition	Combining two parts to make a whole: part whole model. Starting at the bigger number and counting on. Regrouping to make 10.	Adding three single digits. Column method – no regrouping.	Column method- regrouping. (up to 3 digits)	Column method- regrouping. (up to 4 digits)	Column method- regrouping. (with more than 4 digits) (Decimals- with the same amount of decimal places)	Column method- regrouping. (Decimals- with different amounts of decimal places)
Subtraction	Taking away ones Counting back Find the difference Part whole model Make 10	Counting back Find the difference Part whole model Make 10 Column method- no regrouping	Column method with regrouping. (up to 3 digits)	Column method with regrouping. (up to 4 digits)	Column method with regrouping. (with more than 4 digits) (Decimals- with the same amount of decimal places)	Column method with regrouping. (Decimals- with different amounts of decimal places)
Multiplication	Doubling Counting in multiples Arrays (with support)	Doubling Counting in multiples Repeated addition Arrays- showing commutative multiplication	Counting in multiples Repeated addition Arrays- showing commutative multiplication Grid method	Column multiplication (2 and 3 digit multiplied by 1 digit)	Column multiplication (up to 4 digit numbers multiplied by 1 or 2 digits)	Column multiplication (multi digit up to 4 digits by a 2 digit number)
Division	Sharing objects into groups Division as grouping	Division as grouping Division within arrays	Division within arrays Division with a remainder Short division (2 digits by 1 digit- concrete and pictorial)	Division within arrays Division with a remainder Short division (up to 3 digits by 1 digit- concrete and pictorial)	Short division (up to 4 digits by a 1 digit number interpret remainders appropriately for the context)	Short division Long division (up to 4 digits by a 2 digit number- interpret remainders as whole numbers, fractions or round)

# CALCULATION POLICY FOR ADDITION

Key language which should be used: sum, total, parts and wholes, plus, add, altogether, more than, 'is equal to' 'is the same as'.

Concrete	Pictorial	Abstract
Combining two parts to make a whole (use other resources too e.g. shells, teddy bears etc.)	Children to represent the counters using dots.	4 + 3 = 7 (four is a part, 3 is a part and the whole is seven.)
Counting on using number lines by using	A bar model which encourages the children	The abstract number line:
cubes or Numicon.	to count on rather than count all.	What is 2 more than 4?
	4	What is the sum of 2 and 4? What is the total of 4 and 2? 4+2
Regrouping to make 10; using ten frames.	Children to draw the tens frame.	Children to develop an understanding of
6+5		equality. e.g. 6 + - = 11 6 + 5 = 5 + - 6 + 5 = - + 4





# MENTAL CALCULATIONS FOR ADDITION

These are a **selection** of mental calculation strategies: It is very important that children know and can use their number facts.

 Mental recall of number bonds

 6 + 4 = 10  $\Box + 3 = 10$  25 + 75 = 100  $19 + \Box = 20$ 

**Use near doubles** 6 + 7 = double 6 + 1 = 13

Addition using partitioning and recombining 34 + 45 = (30 + 40) + (4 + 5) = 79

Counting on or back in repeated steps of 1, 10, 100, 1000 86 + 57 = 143 (by counting on in tens and then in ones) 460 - 300 = 160 (by counting back in hundreds)

Add the nearest multiple of 10, 100 and 1000 and adjust 24 + 19 = 24 + 20 - 1 = 43 458 + 71 = 458 + 70 + 1 = 529

Use the	relationship	between	addition	and	subtraction
36 + 19 =	= 55		19 + 36	= 55	
55 - 19 =	= 36		55 - 36	= 19	

MANY MENTAL CALCULATION STRATEGIES WILL CONTINUE TO BE USED. THEY ARE NOT REPLACED BY WRITTEN METHODS.

Woodlands Federation – Calculations Policy

# CALCULATION POLICY FOR SUBTRACTION

Key language which should be used: take away, less than, the difference, subtract, minus, fewer, decrease.

Concrete	Pictorial	Abstract
Physically taking away and removing objects from a whole. 4 -3 = 1	Children to draw the concrete resources they are using and cross out. The bar model can also be used.	4 + 3 = 1 $= 4 - 3$ $4$ $3$ $7$ $4$ $4$ $7$ $4$ $7$ $3$
<b>Counting back (</b> using number line or number tracks) Children to start with 6 and count back 2.	Children to represent what they see pictorially.	Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line.
	12345678910	







# MENTAL CALCULATIONS FOR SUBTRACTION

These are a **selection** of mental calculation strategies: It is important that children know and can apply their number facts. Mental recall of addition and subtraction facts 10 - 6 = 4 17 - 🗆 = 11 20 - 17 = 3 10 - 🗆 = 2 Find a small difference by counting up 82 - 79 = 3 Counting on or back in repeated steps of 1, 10, 100, 1000 86 - 52 = 34 (by counting back in tens and then in ones) 460 - 300 = 160 (by counting back in hundreds) Subtract the nearest multiple of 10, 100 and 1000 and adjust 24 - 19 = 24 - 20 + 1 = 5 458 - 71 = 458 - 70 - 1 = 387

Use the relationship between addition and subtraction

36 + 19 = 55	19 + 36 = 55	55 - 19 = 36	55 - 36 = 19

MANY MENTAL CALCULATION STRATEGIES WILL CONTINUE TO BE USED. THEY ARE NOT REPLACED BY WRITTEN METHODS.

# CALCULATION POLICY FOR MULTIPLICATION

Woodlands Federation – Calculations Policy

Key language which should be used: double times, multiplied by, the product of, groups of, lots of.

Concrete	Pictorial	Abstract
Repeated grouping/repeated addition (does not have to be restricted to cubes) 3 x 4 There are 3 equal groups, with 4 in each group. 4+4+4	Children to represent the practical resources in a picture and use a bar model.	3 x 4 = 12 12= 3 x 4 4+4+4 = 12
Number Lines to show repeated groups. 3 × 4	Represent this pictorially alongside a number line e.g.	Abstract number line showing three jumps of four. $3 \times 4 = 12$

Use arrays to illustrate commutativity; (counters and other objects can also be used) $2 \times 5 = 5 \times 2$ $2 \log of 5$ $5 \log of 2$	Children to represent the arrays pictorially.	Children to be able to use an array to write a range of calculations e.g. 10 = 2 × 5 5 × 2 = 10 2 + 2 + 2 + 2 + 2 = 10 10 = 5 + 5
Partition to multiply; using Numicon, base 10 or Cuisenaire rods. 15 × 4	Children to represent the concrete manipulatives pictorially.	Children to be encouraged to show the steps they have taken.

Woodlands Federation – Calculations Policy

Formal Column Method; with place value	Children to represent the counters	Children to record what it is they are
$3 \times 23$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$3 \times 23 \qquad 3 \times 20 = 60$ $3 \times 3 = 9$ $20 \qquad 3 \qquad 60 + 9 = 69$ $23$ $\frac{\times 3}{69}$
Formal Column Method with place value counters. $6 \times 23$ Step 1: get 6 lots of 23         Step 2: $6 \times 3$ is 18. Can I make an exchange? Yes! Ten ones for one ten         Step 3: $6 \times 2$ tens and my extra ten is 13 tens. Can I make an exchange? Yes! Ten tens for one hundred         Step 4- what do I have I each column?	Children to represent the counters/ base 10 pictorially.	$6 \times 23 =$ 23 $\frac{\times 6}{138}$ $\frac{1}{11}$

Woodlands Federation – Calculations Policy

When children start to multiply 3digit $x$ 3 digit and 4 digit $x$ 2 digit they should be confident with the abstract:			124 × 26
To get 744 children have solved 6	6 x 124		7 4 4
To get 2480 they have solved 20	To get 2480 they have solved 20 x 124		
			1 1 Answer: 3224
Conceptud	al Variation, different w	vays to ask children to	o solve 6 x 23
23 23 23 23 23 23 23 ?	Mai had to swim 23 lengths, 6 times a week. How many lengths did she swim in one week?	Find the product of 6 and 23 6 × 23 = []=6 × 23 6 23 × 23 × 6	8. What is the calculation? What is the product?
With the counters, prove that 6 x 23 = 138 Explain why	Tom saved 23p three days a week. How much did he save in 2 weeks?		
6x23= 23 x6			

Woodlands Federation – Calculations Policy

# MENTAL CALCULATIONS FOR MULTIPLICATION

These are a **selection** of mental calculation strategies:

# Doubling and halving

Applying the knowledge of doubles and halves to known facts. e.g.  $8 \times 4$  is double  $4 \times 4$ 

#### Using multiplication facts

**Tables should be taught every day** from Y1 onwards, either as part of the mental oral starter or other times as appropriate within the day. Pupils to be confident using the counting stick and able to recall and use multiplication and division facts.

- Year 1 x2, x5 and x10 tables
- Year 2 x2, x5, x10 and x3 tables
- Year 3 x3, x6, x4 and x8 tables
- Year 4 all tables up to 12 x 12

# Using and applying division facts

Children should be able to utilise their tables knowledge to derive other facts. e.g. If I know  $3 \times 7 = 21$ , what else do I know?  $30 \times 7 = 210$ ,  $300 \times 7 = 2100$ ,  $3000 \times 7 = 21000$ ,  $0.3 \times 7 = 2.1$  etc

# Use closely related facts already known

13 × 11 = (13 × 10) + (13 × 1) = 130 + 13 = 143

Woodlands Federation - Calculations Policy

# Multiplying by 10 or 100

Knowing that the effect of multiplying by 10 is a shift in the digits one place to the left. Knowing that the effect of multiplying by 100 is a shift in the digits two places to the left.

#### Partitioning

23 × 4 = (20 × 4) + (3 × 4) = 80 + 12 = 102

# Use of factors

8 x 12 = 8 x 4 x 3

MANY MENTAL CALCULATION STRATEGIES WILL CONTINUE TO BE USED. THEY ARE NOT REPLACED BY WRITTEN METHODS.

# CALCULATION POLICY FOR DIVISION

Key language which should be used: share, group, divide, divided by, half.

Concrete	Pictorial	Abstract
Sharing using a range of objects. 6 ÷ 2	Represent the sharing pictorially.	6 ÷ 2 = 3 3 3
Repeated subtraction using Cuisenaire rods. $6 \div 2$ $\frac{-2}{2} + \frac{-2}{2} + \frac{-2}{2} + \frac{-2}{2} + \frac{-2}{3} + \frac{-2}{3} + \frac{-2}{5} + $	Children to represent repeated subtraction pictorially.	Abstract number line to represent the equal groups that have been subtracted.

Woodlands Federation – Calculations Policy



Children to represent the counters pictorially. Children to record the calculation Short division (Bus Stop); with place value using the short division scaffold. counters to group.

615 ÷ 5



1. Make 615 with place value counters.

2. How many groups of 5 hundreds can you make with 6 hundred counters?

3. Exchange 1 hundred for 10 tens.

4. How many groups of 5 tens can you make with 11 ten counters?

5. Exchange 1 ten for 10 ones.

6. How many groups of 5 ones can you make with 15 ones?





Woodlands Federation - Calculations Policy



# Long Division:

Concrete	Pictorial	Abstract
2544 ÷ 12 How many groups of 12 thousands do we have? None	Children to represent the counters, pictorially and record the subtractions beneath.	Step one- exchange 2 12 2544 So we now have 25 hundreds,
Exchange 2 thousand for 20 hundreds.		Step two- How many groups of 12 can I make with 25 hundreds? The 24 shows the hundreds we have grouped. The one is how many
How many groups of 12 2544 12 2544 12 2544 12 are in 25 hundreds? 2 groups. Circle them. We have grouped 24 hundreds so can take them off and we are left with one.		hundreds we have left, Exchange the one hundred for 10 tens, How many 24 12 2544 groups of 12 can I make with 14 tens? The 14 shows how many tens
Exchange the one hundred for ten tens so now we have 14 tens, How many arouns of 12 are in 142 1 remainder 2		I have, the 12 is how many I grouped and the 2 is how many tens I have left. 12 2544 24 Exchange the 2 tens for 20 ones. The 24 is how many ones
Exchange the two tens for twenty ones so now we have 24 ones, How many groups of 12 are in 24? 2		14 I have grouped and the 0 is 12 what I have left. 24 24 0

# MENTAL CALCULATIONS FOR DIVISION

These are a **selection** of mental calculation strategies:

# Doubling and halving

Knowing that halving is dividing by 2

# Deriving and recalling division facts

**Tables should be taught every day** from Y1 onwards, either as part of the mental oral starter or other times as appropriate within the day. Pupils to be confident using the counting stick and able to recall and use multiplication and division facts.

#### Using and applying division facts

Children should be able to utilise their tables knowledge to derive other facts. e.g. If I know 3 x 7 = 21, what else do I know?

21 ÷ 3 = 7 21 ÷ 7 = 3 3 = 21 ÷ 7 and 7 = 21 ÷ 3

# Dividing by 10 or 100

Knowing that the effect of dividing by 10 is a shift in the digits one place to the right.

Knowing that the effect of dividing by 100 is a shift in the digits two places to the right.

#### Use of factors

 378 ÷ 21
 378 ÷ 3 = 126
 378 ÷ 21 = 18
 126 ÷ 7 = 18

# Use related facts

Given that 1.4 × 1.1 = 1.54

What is 1.54 ÷ 1.4, or 1.54 ÷ 1.1?

Woodlands Federation -	- Calculations Policy
------------------------	-----------------------